

FIRM:Your Firm  
MADE BY:KJH DATE:05-21-2006  
TITLE:Example ABUTMENT calculation

JOB NO.  
CHECKED BY:

SHEET NO: 1  
DATE:

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ABUTMENT DESIGN:  
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DESIGN DATA:  
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Design Method: Load Factor Design  
Dead Load Factor=1.39  
Live Load Factor=1.70  
Earth Pressure Load Factor=1.70

Concrete strength,  $f_c' = 3.50$  ksi  
Reinforcing,  $F_y = 60$  ksi

Minimum reinforcing steel ratio,  $p_{min} = 0.00132$  (on gross area)

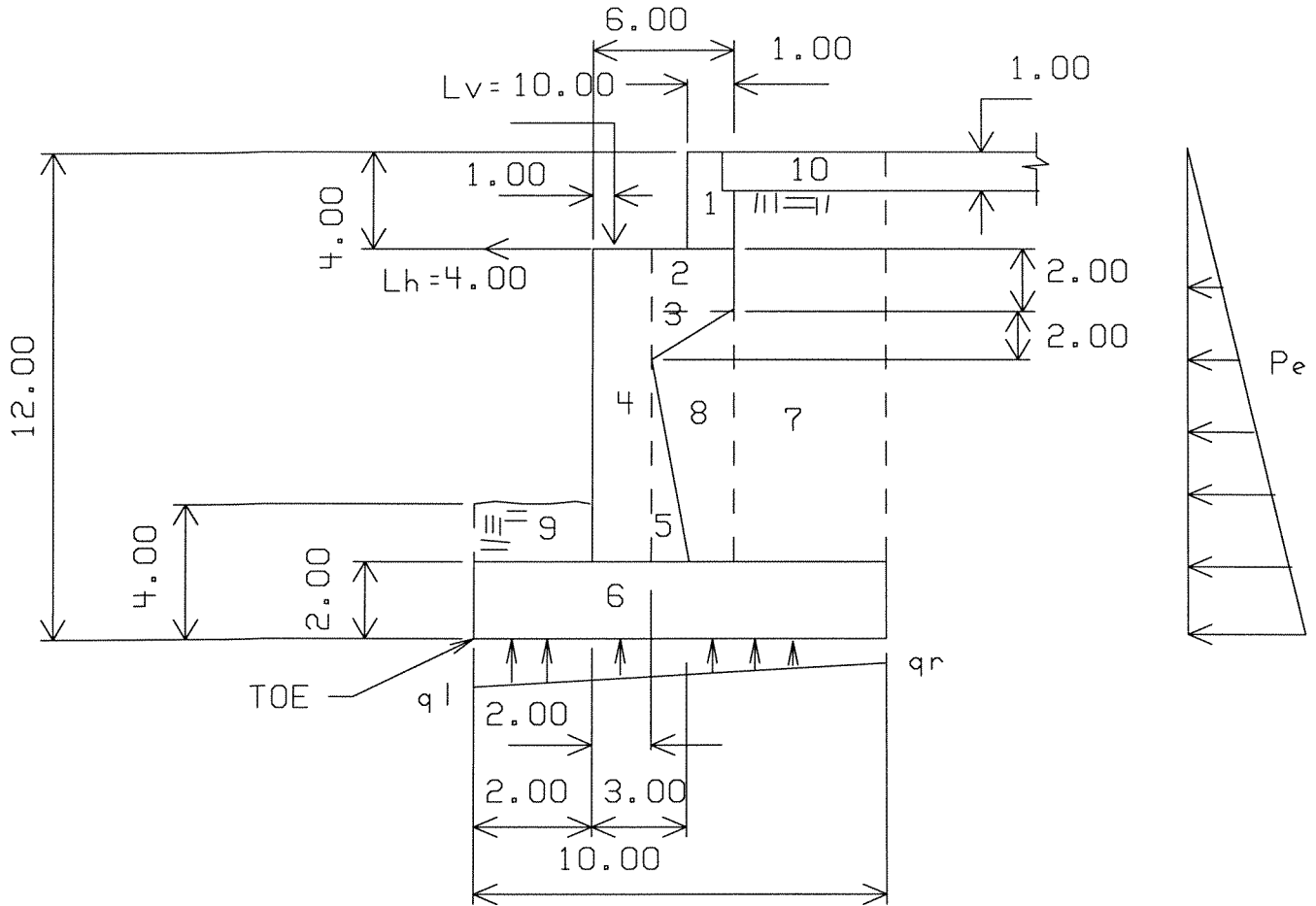
Bar clearances: 3.00 inches for bars cast above grade  
2.00 inches for other bars

Soil behind wall is unsaturated. Dry earth weight = .119 kcf  
Angle of internal friction= 30.00 degrees

Design for active earth pressure:  
 $K_a = [1 - \sin(30.00)] / [1 + \sin(30.00)] = .333$   
 $P_a = .333 \times .119 = 0.040$  kcf

For sliding check of spread footings (see '91 AASHTO Table 5.5.5B):  
Interface: Clean silty or clayey gravel  
Friction factor= .449  
Adhesion = 0.000 ksf

ABUTMENT DESIGN:



STABILITY ANALYSIS:

Item	V	H	arm	Mtoe
1: 1.00 X 4.00 X .15 =	.6		7.50	4.5
2: 4.00 X 2.00 X .15 =	1.2		6.00	7.2
3: 1/2 X 4.00 X 2.00 X .15 =	.6		5.33	3.2
4: 2.00 X 6.00 X .15 =	1.7		3.00	5.3
5: 1/2 X 1.00 X 2.00 X .15 =	.1		4.33	.6
6: 10.00 X 2.00 X .15 =	3.0		5.00	15.0
7: 2.00 X 9.00 X .119 =	2.1		9.00	19.4
8:	1.3		6.39	8.4
9: 2.00 X 2.00 X .119 =	.4		1.00	.4
10: 2.00 X 1.00 X .15 =	.3		9.00	2.7
Lv:	10.0		3.00	30.0
Lh:		4.0	-8.00	-32.0
Pe: 1/2x ( 11.0) <sup>2</sup> x 0.040 =		2.4	-3.66	-8.8
Ps: 1.00 x .15x .333 x 11.00 =		.5	-5.50	-3.0
TOTALS =	21.6	6.9		53.1

Eccentricity, e = 53.1/ 21.6 = 2.45 feet right of toe

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$e < W/2 = 5.000$ , therefore footing uplifts

Length of pressure triangle =  $3 \times 2.457 = 7.373$

$21.6 = 1/2 \times 7.373 \times q_1$   
 $q_1 = 2 \times 21.6 / 7.373 = 5.861$  ksf

CHECK OVERTURNING WITHOUT SUPERSTRUCTURE IN PLACE:  
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Overturning moment, $M_o =$	3.02+	8.87=	11.89	k*ft
Righting moment, $M_r =$	4.50 +	7.20 +	3.20 +	5.39
	+ .65 +	15.00 +	19.43 +	8.43
	+ .47+	2.70 =	67.00	k*ft

Safety factor against overturning,  
 $SF = M_r / M_o = 67.00 / 11.89 = 5.631$

CHECK SLIDING:  
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Available friction at base =  $.449 \times 21.6 \text{ k} + 0.000 \times 10.00' = 9.72 \text{ k}$

$K_p = (1 + \sin 30.00) / (1 - \sin 30.00) = 2.99$

$P_p = .119 \times 2.99 = .359$  kcf

Available passive pressure in front =  $1/2 \times .359 \text{ ksf} \times (4.000 \text{ ft})^2 = 2.87 \text{ k}$

Safety factor against sliding (w/o passive pressure)  
=  $9.72 / 6.9 = 1.395$

Safety factor against sliding (w/passive pressure)  
=  $(9.72 + 2.87) / 6.9 = 1.808$

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COMPUTE FACTORED FOOTING PRESSURES FOR FOOTING DESIGN:

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For footing design purposes, linear contact pressures are computed based on the factored loads (see AASHTO Standard Spec. 5.14.7).

Factoring forces and moments from stability analysis:

$$\begin{aligned} V_{\text{factored}} &= ( .60 + 1.20 + .60 + 1.79 + .15 + 3.00 + 2.15 \\ &\quad + 1.31 + .47 + .30 + 0.00 ) \times 1.39 \quad \text{(Dead loads)} \\ &\quad + 10.00 \times 1.70 \quad \text{(Live load)} \\ &= 33.25 \text{ k/ft} \end{aligned}$$

$$\begin{aligned} H_{\text{factored}} &= ( .55 + 2.42 ) \times 1.70 \quad \text{(Earth loads)} \\ &\quad + 4.00 \times 1.70 \quad \text{(Live load)} \\ &= 11.84 \text{ k/ft} \end{aligned}$$

$$\begin{aligned} M_{\text{factored}} &= ( 4.50 + 7.20 + 3.20 + 5.39 + .65 + 15.00 + 19.43 \\ &\quad + 8.43 + .47 + 2.70 + 0.00 ) \times 1.39 \quad \text{(Dead loads)} \\ &\quad + ( -3.02 + -8.87 ) \times 1.70 \quad \text{(Earth loads)} \\ &\quad + ( 30.00 + -32.00 ) \times 1.70 \quad \text{(Live load)} \\ &= 70.1 \text{ k*ft/ft} \end{aligned}$$

Eccentricity due to factored loads,  
 $e = 70.1 / 33.2 = 2.11$  feet right of toe

$e < W/2 = 5.000$ , therefore footing uplifts

Length of pressure triangle =  $3 \times 2.110 = 6.331$

$$\begin{aligned} 33.2 &= 1/2 \times 6.331 \times q_1 \\ \text{Factored } q_1 &= 2 \times 33.2 / 6.331 = 10.503 \text{ ksf} \end{aligned}$$

COMPUTE FACTORED FOOTING PRESSURES FOR BEARING CAPACITY FAILURE CHECK:

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Customarily, service load pressures (see previous sheet) have been checked against allowable bearing pressures. With the introduction of LF/LRFD design approaches, a check of factored pressure compared to ultimate bearing capacity is also required (see AASHTO Standard Spec. 5.14.6.1 and LRFD Art. 10.6.2.2.4).

To check against bearing capacity failure, a uniform contact pressure acting over an effective width equal to "B - 2\*e" is computed using the factored loads.

Footing width, B = 7.37 ft  
Eccentricity to center of footing,  $e = 7.37 \text{ ft} / 2 - 2.11 \text{ ft} = 1.57 \text{ ft}$   
Effective contact width,  $B - 2*e = 7.37 \text{ ft} - 2*1.57 \text{ ft} = 4.22 \text{ ft}$

$$\text{Uniform factored pressure, } q_{\text{max}} = 33.2 \text{ k/ft} / 4.22 \text{ ft} = 7.87 \text{ ksf}$$

(The designer will need to check " $q_{\text{max}}$ " against the reduced " $q_{\text{ult}}$ " specific to geotechnical information at this location.)

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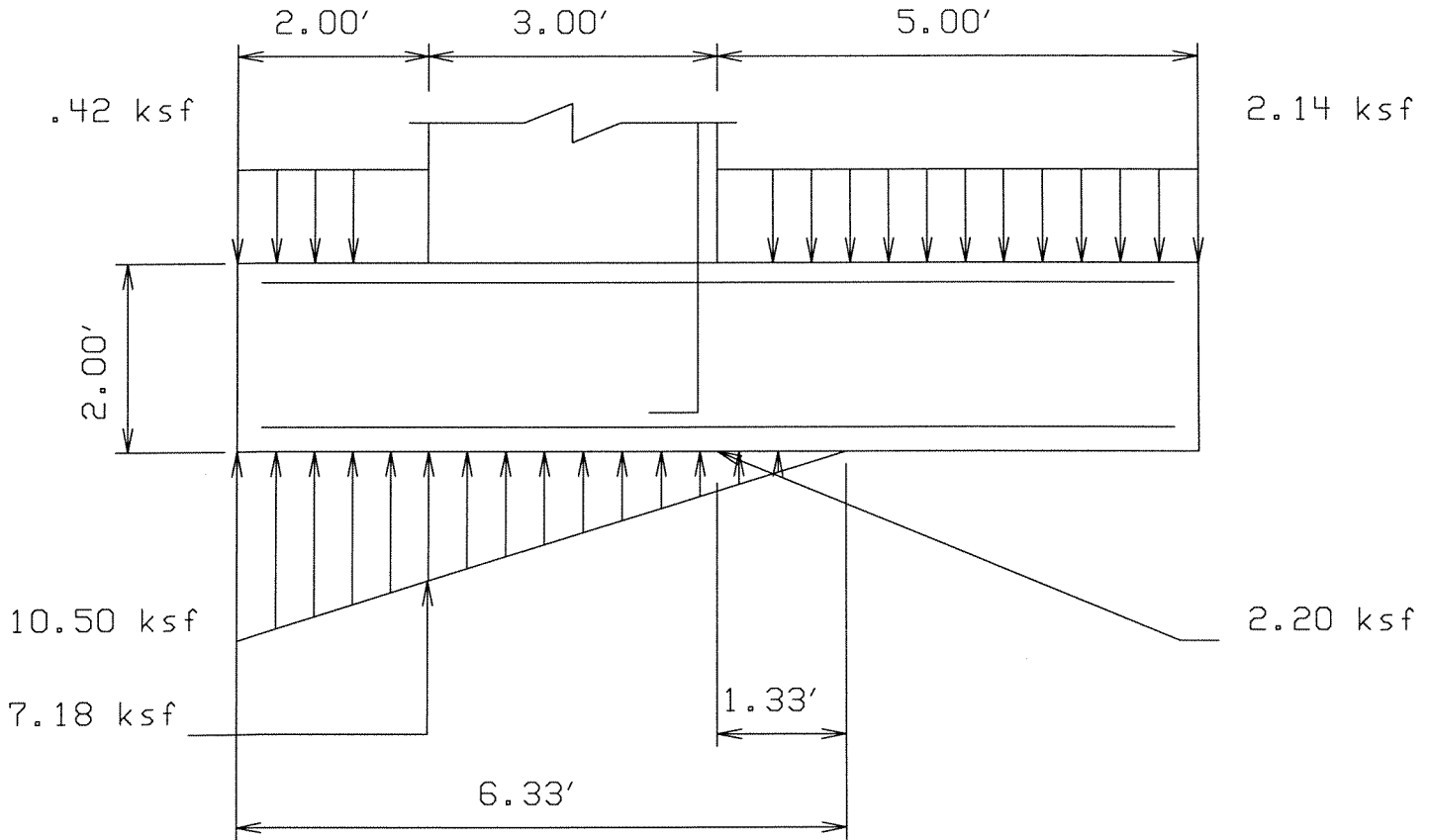
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ABUTMENT DESIGN:

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FOOTING DESIGN DATA:

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Minimum reinforcement ratio=0.0013 (on gross area)  
 $F_y = 60.00$  ksi,  $f_c' = 3.50$  ksi  
 Allowable shear=  $0.85 * 2 (3500)^{.5} = 100$  psi

$d = 12 \times 2.00 - (3.00 + 0.5)$  in= 20.50 in (bottom bars)  
 $= 12 \times 2.00 - (2.00 + 0.5)$  in= 21.50 in (top bars)

LOADS ON TOP OF FOOTING:

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Load on toe,  
 (Neglect overburden on toe, due to possibility of erosion)  
 Dead load footing=  $2.00 \times 0.15 = .30$  ksf  
 Factored dead load footing =  $1.39 \times .30$  ksf =  $.42$  ksf

Load on heel,  
 $= (12.00 - 2.00 - 1.00) \times .119$  kcf +  $1.00 \times .15 + .30$  ksf=  $1.52$  ksf  
 Factored load on heel =  $1.39 \times 1.52$  ksf =  $2.14$  ksf

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ABUTMENT DESIGN:

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TOE DESIGN:

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$$\text{Factored } M_{dlU} = .42 \times (2.00)^2 / 2 = .84 \text{ k*ft/ft}$$

$$\text{Critical section for shear at } 2.00 \text{ ft} - 20.50 \text{ in} / 12 = .29 \text{ ft from toe}$$
$$\text{Factored } V_{dlU} = .42 \times .29 = .12 \text{ k/ft}$$

Compute factored toe moment and shear due to factored footing pressures:

$$M_{qU} = 7.18 \times (2.00)^2 / 2 + 1/3 \times (10.50 - 7.18) \times (2.00)^2 = 18.79 \text{ k*ft}$$

$$\text{At critical shear section, } q = 10.50 - .29 \times 10.50 / 6.33 = 10.01 \text{ k}$$
$$V_{qU} = 10.01 \times .29 + 1/2 \times (10.50 - 10.01) \times .29 = 2.99 \text{ k}$$

$$\text{Total factored shear, } V_u = 2.99 - .12 = 2.87 \text{ k}$$
$$\text{Shear stress} = 2.87 / (12 \times 20.50) \times 1000 = 11 \text{ psi} < 100 \text{ psi (OK)}$$

$$\text{Factored moment, } M_u = 18.79 - .84 = 17.95 \text{ k*ft}$$

By trial and error, compression block depth,  $a = .32 \text{ in}$

$$A_s = 12 \times M / (0.9 \times F_y (d - a/2))$$
$$= 12 \times 17.9 / (0.9 \times 60 (20.50 - .32/2))$$
$$= .19 \text{ in}^2 / \text{ft}$$

Check a:

$$a = A_s \times F_y / (0.85 \times F_c \times b)$$
$$= .19 \times 60.00 / (0.85 \times 3.50 \times 12)$$
$$= .32 \text{ in (checks)}$$

Minimum reinforcement,

$$A_{min} = 200 / 60000 \times 20.50 \times 12 = .81 \text{ in}^2 / \text{ft}$$

or  $= 1.33 \times .19 = .26 \text{ in}^2 / \text{ft}$

but not less than,  $0.0013 \times 24.00 \times 12 = .38 \text{ in}^2 / \text{ft}$

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| Toe reinforcement req'd = .38 sq.in./ft Bot. |

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ABUTMENT DESIGN:

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HEEL DESIGN:

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$$\text{Factored MdlU} = 1/2 \times 2.14 \times (5.00)^2 = 26.77 \text{ k*ft}$$

$$\text{Factored VdlU} = 2.14 \times 5.00 = 10.71 \text{ k/ft}$$

Factored heel moment and shear due to factored footing pressures:

$$\text{MqU} = 1/6 \times 2.20 \times (1.33)^2 = .6 \text{ k*ft}$$

$$\text{VqU} = 1/2 \times 2.20 \times 1.33 = 1.47 \text{ k}$$

$$\text{VUtot} = 10.71 - 1.47 = 9.23 \text{ k}$$

$$\text{Shear stress} = 9.23 / (12 \times 21.50) \times 1000 = 35 \text{ psi} < 100 \text{ psi (OK)}$$

$$\text{Factored moment, Mu} = .65 - 26.77 = -26.12 \text{ k*ft}$$

By trial and error, compression block depth, a = .45 in

$$\begin{aligned} \text{As} &= 12 \times \text{M} / (0.9 \times \text{Fy} (\text{d} - \text{a}/2)) \\ &= 12 \times 26.1 / (0.9 \times 60 (21.50 - .45/2)) \\ &= .27 \text{ in}^2 / \text{ft} \end{aligned}$$

Check a:

$$\begin{aligned} \text{a} &= \text{As} \times \text{Fy} / (0.85 \times \text{Fc} \times \text{b}) \\ &= .27 \times 60.00 / (0.85 \times 3.50 \times 12) \\ &= .45 \text{ in (checks)} \end{aligned}$$

Minimum reinforcement,

$$\begin{aligned} \text{Amin} &= 200 / 60000 \times 21.50 \times 12 = .86 \text{ in}^2 / \text{ft} \\ \text{or} &= 1.33 \times .27 = .36 \text{ in}^2 / \text{ft} \\ \text{but not less than, } &0.0013 \times 24.00 \times 12 = .38 \text{ in}^2 / \text{ft} \end{aligned}$$

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| Heel reinforcement req'd = .38 sq.in./ft Top |

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ABUTMENT DESIGN:

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HEEL DESIGN (Cont'd):

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ALTERNATE LOADING CASE:

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Calculate reinforcement required for moment due to loads above the footing only. This condition will correspond roughly to when the abutment is backfilled without superstructure or with little or no live load. Use an arbitrary reduced load factor, LF=1.3:

$$\text{Alternate Mu} = -1.3 \times 1/2 \times (1.52 \text{ ksf}) \times (5.00)^2 = -24.86 \text{ k*ft}$$

By trial and error, compression block depth,  $a = .43 \text{ in}$

$$\begin{aligned} A_s &= 12 * M / (0.9 * F_y (d - a/2)) \\ &= 12 \times 24.8 / (0.9 \times 60 (21.50 - .43/2)) \\ &= .25 \text{ in}^2 / \text{ft} \end{aligned}$$

Check a:

$$\begin{aligned} a &= A_s * F_y / (0.85 \times F_c \times b) \\ &= .25 \times 60.00 / (0.85 \times 3.50 \times 12) \\ &= .43 \text{ in (checks)} \end{aligned}$$

Minimum reinforcement,

$$\begin{aligned} A_{min} &= 200 / 60000 \times 21.50 \times 12 = .86 \text{ in}^2 / \text{ft} \\ \text{or} &= 1.33 \times .25 = .34 \text{ in}^2 / \text{ft} \\ \text{but not less than, } &0.0013 \times 24.00 \times 12 = .38 \text{ in}^2 / \text{ft} \end{aligned}$$

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| Heel reinforcement req'd= .38 sq.in./ft Top |

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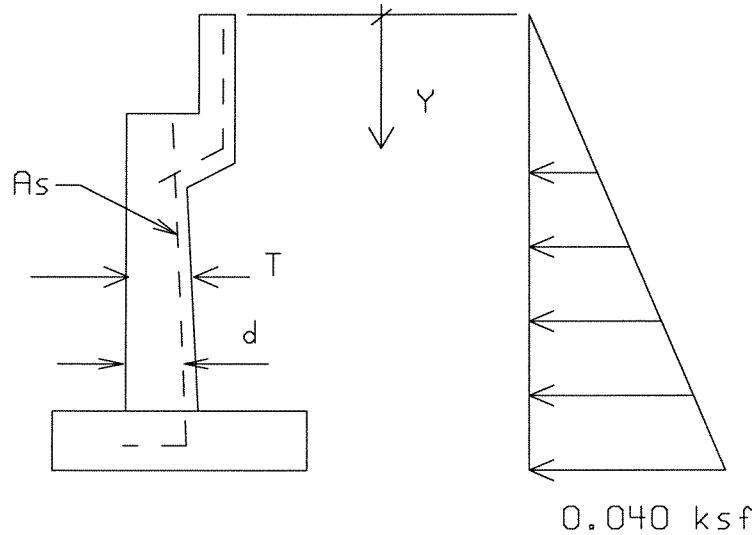
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ABUTMENT DESIGN:

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STEM DESIGN - BACK FACE BARS:

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Load factor for stem design=1.70

Distance from center of bars to back face = 2.00 + 0.5 in.= 2.50 in

y (ft)	M (k*ft)	Mu (k*ft)	t (in)	d (in)	Reinforcement in back face (sq. in/ft)				
					As, req'd	4/3xAs Min.	Min ratio 200/Fy	Min. ratio 0.0013	Use As
0.0	0.0	0.0	12.00	9.50	0.00	0.00	.37	.19	.19
1.0	0.0	0.0	12.00	9.50	0.00	0.00	.37	.19	.19
2.0	0.0	.0	12.00	9.50	0.00	0.00	.37	.19	.19
3.0	.1	.3	12.00	9.50	0.00	0.00	.37	.19	.19
4.0	.4	.7	12.00	9.50	0.01	0.02	.37	.19	.19
5.0	.8	1.4	72.00	69.50	0.00	0.00	2.77	1.14	1.14
6.0	1.4	2.4	72.00	69.50	0.00	0.01	2.77	1.14	1.14
7.0	2.2	3.8	48.00	45.50	0.01	.02	1.82	.76	.76
8.0	3.4	5.8	24.00	21.50	0.06	0.07	.86	.38	.38
9.0	4.8	8.2	30.00	27.50	0.06	0.08	1.10	.47	.47
10.0	6.6	11.3	36.00	33.50	0.07	.10	1.34	.57	.57

Shear at base of stem= $1/2 \times (10.0)^2 \times 0.040 = 2.00$  k

$V_u = 1.70 \times 2.00 = 3.40$  k

$f_v = 3.40 / (12 \times 33.50) \times 1000 = 8$  psi <  $f_v, \text{allowable} = 100$  psi (OK)

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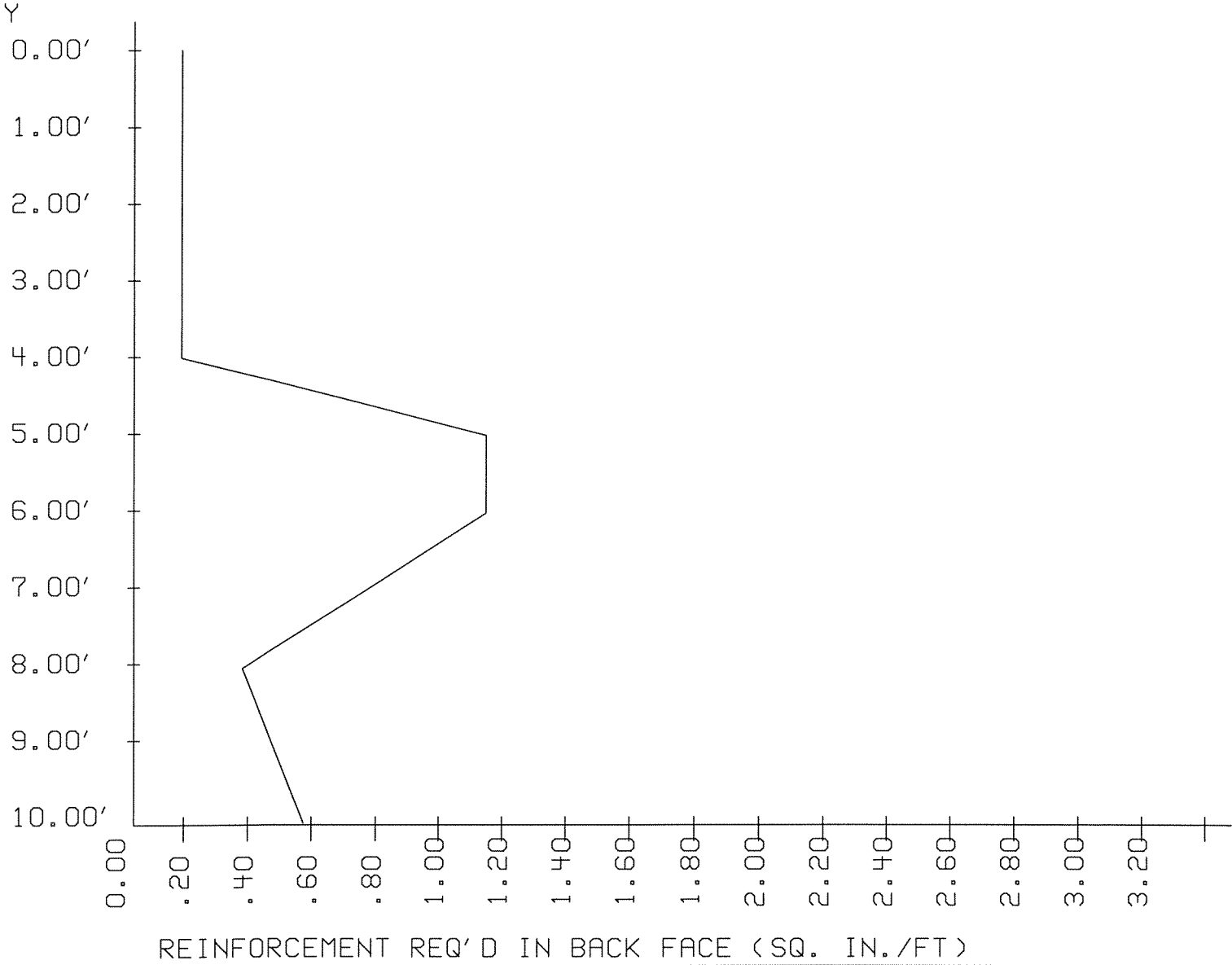
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ABUTMENT DESIGN:

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STEM DESIGN - BACK FACE BARS:

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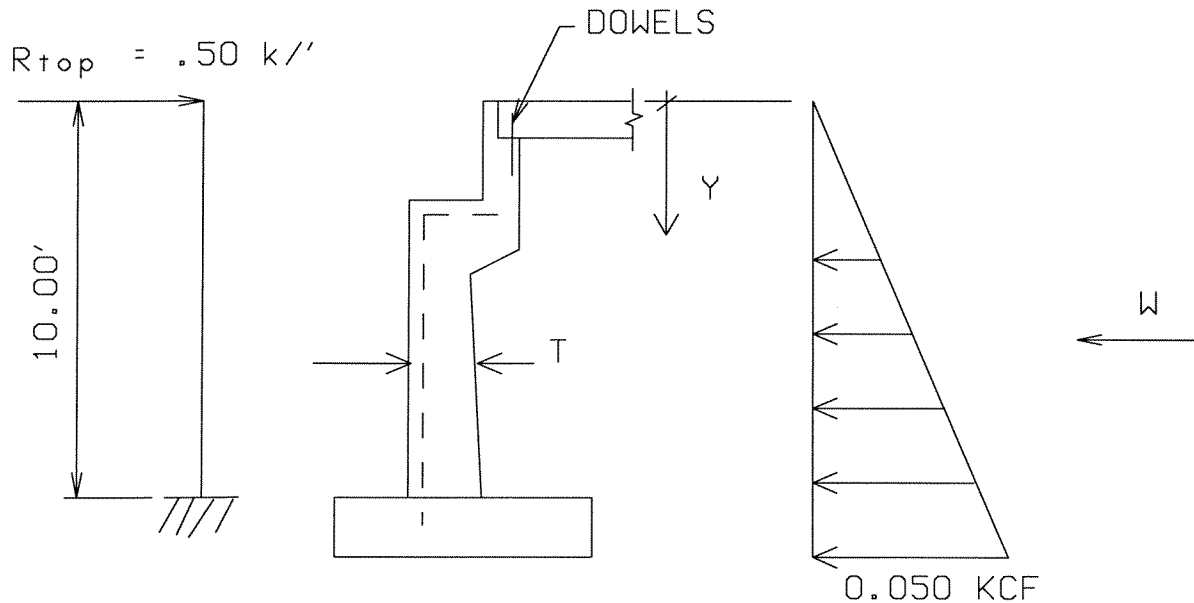
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ABUTMENT DESIGN:

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STEM DESIGN - FRONT FACE BARS:

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With time, creep and settlement in the fill will cause the abutment to act as a pinned-fixed structure. Pressures will tend to increase towards the at-rest state. Arbitrarily design for 125% of active pressure:  $125\% * 0.040 \text{ kcf} = 0.050 \text{ kcf}$

Load factor for stem design=1.70

Distance from center of bars to front face =  $2.00 + 0.5 \text{ in.} = 2.50 \text{ in}$

y (ft)	M (k*ft)	Mu (k*ft)	t (in)	d (in)	Reinforcement in front face (sq. in/ft)				
					As, req'd	4/3xAs Min.	Min ratio 200/Fy	Min. ratio 0.0013 (*)	Use As*
0.0	0.0	0.0	12.00	9.50	0.00	0.00	.37	(*)	0.00
1.0	.4	.8	12.00	9.50	0.01	0.02	.37	(*)	0.02
2.0	.9	1.5	12.00	9.50	.03	0.04	.37	(*)	0.04
3.0	1.2	2.1	12.00	9.50	0.05	0.06	.37	(*)	0.06
4.0	1.4	2.4	12.00	9.50	0.05	0.07	.37	(*)	0.07
5.0	1.4	2.4	72.00	69.50	0.00	0.01	2.77	(*)	0.01
6.0	1.2	2.0	72.00	69.50	0.00	0.00	2.77	(*)	0.00
7.0	.6	1.0	48.00	45.50	0.00	0.00	1.82	(*)	0.00
8.0	-.2	-.4	24.00	21.50	0.00	0.00	.86	(*)	0.00
9.0	-1.5	-2.6	30.00	27.50	0.00	0.00	1.10	(*)	0.00
10.0	-3.3	-5.6	36.00	33.50	0.00	0.00	1.34	(*)	0.00

(\* - NOTE: Designer should evaluate if the 0.0013 minimum ratio applies for this condition.)

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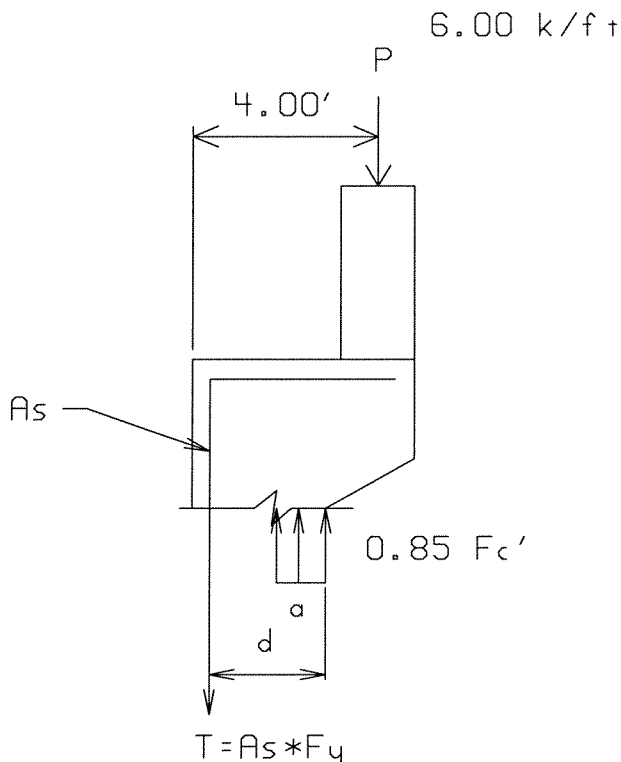
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ABUTMENT DESIGN:

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STEM DESIGN - FRONT FACE BARS:

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Design front face bars to resist load on backwall (neglect other forces)

Use load factor = 1.70

$$P = 1.70 * 6.00 \text{ k/ft} = 10.20 \text{ k/ft}$$

$$d = 12 * 2.00 \text{ ft} - (2.00 + .5) \text{ in} = 21.50 \text{ in}$$

$$e = 12 * 4.00 \text{ ft} - (2.00 + .5) \text{ in} = 45.50 \text{ in (measured from P to front bars)}$$

$$\text{Concrete compression force, } F_{\text{comp}} = P * e / (d - a/2)$$

$$\text{Also, } F_{\text{comp}} = 0.85 * f_c' * a * 12$$

$$\text{By trial and error, } a = .61 \text{ in}$$

$$\text{therefore, } F_{\text{comp}} = 10.20 * 45.50 / (21.50 - .61/2) = 21.89 \text{ k/ft}$$

$$\text{Check } a = 21.8 / (0.85 * 3.50 \text{ ksi} * 12) = .61 \text{ in}$$

$$\text{Force in steel, } T = F_{\text{comp}} - P = 21.89 - 10.20 = 11.69 \text{ k/ft}$$

$$\text{Using 0.9 strength reduction factor, design for } T = 11.69 / 0.9 = 12.99 \text{ k/ft}$$

$$\text{Required area of steel} = T / F_y = 12.99 / 60 = .21 \text{ sq. in./per ft.}$$

Minimum reinforcement,

$$A_{\text{min}} = 200 / 60000 * 21.50 * 12 = .86 \text{ in}^2 / \text{ft}$$

$$\text{or } = 1.33 * .21 = .28 \text{ in}^2 / \text{ft}$$

$$\text{but not less than, } 0.0013 * 24.00 * 12 = .38 \text{ in}^2 / \text{ft}$$

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| Front face reinforcement req'd = .38 sq. in./ft |

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